

## Worksheet for Quiz 7 (and Exam 3)

→ Italicized parts are optional; I recommend skipping them.

• Here is a way to understand the calculation of molar mass: If you imagine "ripping apart" 1 mole of  $C_5H_{12}$  into atoms, you'll have 5 moles of C + 12 moles of H, so "molar mass" is  $(5 \text{ mol C})(12 \text{ g/mol}) + (12 \text{ mol H})(1 \text{ g/mol}) = 72 \text{ g/mol}$ , with 60 g of C + 12 g of H = 72 g  $C_5H_{12}$

• An **amount** can be described as number, mass, or volume. Dr L wants you to be able to think logically about amounts by mentally visualizing relative amounts and using analogies with everyday objects that are lightweight and heavyweight. If you have 1000 tennis balls and 1000 bowling balls (same number of each) which has larger mass? And if you have 9000 g of tennis balls and 9000 g of bowling balls (same mass) do you see why there is a larger number of tennis balls? You can use similar logic for atoms & molecules, IF you develop a clear idea of which atoms are relatively light and heavy, and think clearly about the implications.

**1a.** For example, consider  $H_2$  (2 g/mol) and  $O_2$  (32 g/mol). If you have the same number of each (like 3.27 mol of  $H_2$  and 3.27 mol of  $O_2$ ) which will have a larger mass, and by what ratio-factor? (By what number do you multiply "mass of  $H_2$ " to get "mass of  $O_2$ "? Or vice versa, by what factor do you need to multiply "mass of  $O_2$ " to get "mass of  $H_2$ "?)

**1b.** If you have equal mass of each (such as 4.87 g  $H_2$ , 4.87 g  $O_2$ ), which sample has a larger number of atoms, and by what multiplicative ratio-factor? {1a-1b answers are below} note: You can do 1a & 1b with intuitive visualizing-logic, or with mathematical-logic by actually doing the math and developing intuitive math-logic by asking, "does dividing by a larger number make the result smaller (compared with dividing by a small number) or larger?" And does dividing by a small number make the result relatively larger (yes, it does) or smaller (no, it doesn't). Compare  $64/32 (=2)$  and  $64/4 (=16)$  and  $64/.4 (=160)$ ; the result is literally larger when you divide by a number  $< 1$ , as when dividing 64 by .4 (which is  $< 1$ ) gives 160, which is larger than 64.

• You can use similar "intuitive logic" for amounts of molecules in chemical reactions. For example, let's look at this reaction:  $1 C_5H_{12} + 8 O_2 \rightarrow 5 CO_2 + 6 H_2O$ . We can think of this rxn at the level of molecules, or scaled-up by a factor of a million, or a mole, or by any other number; "million" is a word that means a large number ( $1,000,000 = 1 \times 10^6$ ) and "mole" is a word that means a much larger number ( $6.02 \times 10^{23}$ ). If we "scale up" a reaction by any number-factor, the AMOUNTS change but RATIOS remain the same. The reaction ratios (1-to-8-to-5-to-6) are the same whether 1 molecule of  $C_5H_{12}$  produces 5 molecules of  $CO_2$  or if 1 mole of  $C_5H_{12}$  produces 5 moles of  $CO_2$ . This idea of "RATIOS remaining the same when AMOUNTS are scaled-up" is a key to thinking about chemical reactions, and mastering chemistry calculations.

• Or mass can be scaled-up from grams to kilograms, pounds, or tons, with conversion factors: metric ( $1000 \text{ g} = 1 \text{ kg}$ ), non-metric ( $454 \text{ g} = 1 \text{ lb}$ ,  $2000 \text{ lbs} = 1 \text{ ton}$ ). If 2.35 g is scaled-up by  $\times 454$  (making its mass 454 times larger) the math is  $(235 \text{ g})(\times 454) / 454 \text{ g}$  so it's now 235 lb. "1 lb / 454 g" is a conversion factor (describing the same thing in two ways, so it = 1 because top & bottom are equal) but the scaling-factor ( $\times 454$ ) actually makes the amount larger.

**1a.**  $O_2$  has more mass, by factor of  $32/2 = 16$ ,  $H_2$  has less ( $1/16$ ).  
**1b.** There is more  $H_2$  by a factor of  $32/2 = 16$ , as in Problem 4.

• These equations describe the same amounts in two ways,  
 $1 \text{ mole } C_5H_{12} + 8 \text{ moles } O_2 \rightarrow 5 \text{ moles } CO_2 + 6 \text{ moles } H_2O$   
 $72 \text{ g } C_5H_{12} + 256 \text{ g } O_2 \rightarrow 220 \text{ g } CO_2 + 108 \text{ g } H_2O$   
because "8 moles  $O_2$ " is the same as "256 g  $O_2$ " (they're just different ways to describe the same amount of  $O_2$ ) and so on.  
 $72 \text{ g } C_5H_{12} + 256 \text{ g } O_2 \rightarrow 220 \text{ g } CO_2 + 108 \text{ g } H_2O$   
 $72 \text{ lbs } C_5H_{12} + 256 \text{ lbs } O_2 \rightarrow 220 \text{ lbs } CO_2 + 108 \text{ lbs } H_2O$   
 $72 \text{ tons } C_5H_{12} + 256 \text{ tons } O_2 \rightarrow 220 \text{ tons } CO_2 + 108 \text{ tons } H_2O$   
Compared with the first two equations (1 mole... and 72 g...) the final two equations (72 lbs... and 72 tons...) are scaled-up by 454 and  $454 \times 2000$  so they have different AMOUNTS, and "8 mole  $O_2 = 256 \text{ lbs } O_2$ " is false; but all 4 equations have the same RATIOS: "mass  $CO_2$  produced / mass  $C_5H_{12}$  reacting" =  $(220 \text{ g} / 72 \text{ g}) = (220 \text{ lbs} / 72 \text{ lbs}) = (220 \text{ tons} / 72 \text{ tons}) = 3.06$ , and their "constant ratio" is useful for doing problems like this:

**2a.** In a complete combustion of 43.8 grams  $C_5H_{12}$ , what mass of  $CO_2$  (in g) is produced? **2b.** In the complete combustion of 43.8 tons  $C_5H_{12}$ , what weight of  $CO_2$  (in tons) is produced? **2a.**  $(43.8 \text{ g } C_5H_{12}) (1 \text{ mol } C_5H_{12} / 72 \text{ g } C_5H_{12}) (5 \text{ mol } CO_2 / 1 \text{ mol } C_5H_{12}) (44 \text{ g } CO_2 / 1 \text{ mol } CO_2) = 134 \text{ g } CO_2$ . **2b.** An easy solution is to "scale up" the reaction from grams to tons, so if 43.8 g  $C_5H_{12}$  produces 134 g  $CO_2$ , then 43.8 tons  $C_5H_{12}$  will produce 134 tons  $CO_2$ . Or, if you convert from tons into grams, work the problem (as in 2a) with g, and then convert from grams back to tons, you'll see 2000 & 454 each used twice, once on fraction-top and once on fraction-bottom, so the 2000's and 454's "cancel" and the only remaining numbers are those in the 2a solution:  $43.8 (1/72) (5/1) (44/1)$ . For more practice, do problems 6a-6b.

**3a.** What weight of  $CO_2$  (~~in~~ <sup>in grams &</sup> pounds) is produced by complete combustion of 1 gallon of gasoline? (1 gallon = 3785 mL; assume gasoline is pure octane;  $C_8H_{18}$  density = .70 g/mL) [answer is 18.0 lbs; a solution-setup is at end of worksheet] = 8180 g

**3b.** Solve 3a using info from Sceptical Chymist 3.18 (pg 130), "a clean-burning automobile engine will emit about 5 lb of C in the form of  $CO_2$  for every gallon of gasoline it consumes."  
**3b:** If an engine emits "5 lb of C in the form of  $CO_2$ " it will emit more than 5 lbs of  $CO_2$  by a factor of  $(44 \text{ g } CO_2 / 12 \text{ g } C)$  which — because a mass-ratio between molecules (as in 2a) or within a molecule (here) is the same whether masses are in g or lbs — is also  $(44 \text{ lb } CO_2 / 12 \text{ lb } C)$ , so  $(5 \text{ lbs } C) (44 \text{ lb } CO_2 / 12 \text{ lb } C) = 18 \text{ lbs } CO_2$  emitted, same as in 3a.

### Problem-Solving Tips

Almost always, if grams are "given" you will convert this to moles by using moles/gram; and if moles are "given" you will convert this to grams by using grams/mole. For example, in #2a "g/mol" is used twice (flipped & as-is) and in-between you use the mole/mole reaction-ratio to convert from moles of what you are GIVEN into moles of what you are asked to FIND.

If you are asked to find an AMOUNT, you **must** begin with an AMOUNT, and then use conversion factors (= 1) to convert it into a different description of the same AMOUNT.

If you are asked to find a RATIO, either you can begin with a RATIO or (more commonly) use the "miles/hour strategy" as in this example: if you know that a sample of n-octane has mass = 265 g, and volume = 379 mL, to find its density in g/mL you divide the g by mL,  $(265 \text{ g} / 379 \text{ mL}) = .699 \text{ g/mL}$ .

4. 64 g of oxygen gas is \_\_\_ mol, 64 g hydrogen gas is \_\_\_ mol. The key idea here is that "oxygen gas" means "the naturally occurring form of oxygen" which is diatomic  $O_2$  not just O. Which 7 gases are diatomic? (He Ne, ... are monotomic gas); memory - HAH (Hydrogen Air Halogens, 124), BrINC1HOF.

**5a.** What is the mass of 234 mL n- $C_8H_{18}$ ? (density = .70 g/mL)  
**5b.** What is the volume of 164 g of n- $C_8H_{18}$ ? [mL  $\leftrightarrow$  g]  
**5c.** If 234 mL of n- $C_8H_{18}$  is 164 g of it, what is its density?