Table 1: a simple Activity-and-Experience Grid

|  | student activities |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| science experiences |  |  |  |  |  |
| $\# 1$ | $\# 2$ | $\# 3$ | $\# 4$ | $\# 5$ |  |
| A. design experiment | - | - | - | yes | yes |
| B. do experiment, make observations | yes | yes | - | - | yes |
| C. hypothetico-deductive reasoning | - | yes | yes | - | yes |
| D. invent theories | - | - | yes | - | yes |

Table 2: Science Experiences, based on a model of 'Integrated Scientific Method'

|  | SCIENCE EXPERIENCES | science experiences are discussed in sections: |
| :---: | :---: | :---: |
| 1a | - Preparation for content, process; backward-reaching, forward-reaching | $2.71_{\mathrm{F}}, 2.72_{\mathrm{B}, \mathrm{F}}, 2.73_{\mathrm{B}}$ |
| 1b | - Posing of an area to study, and of constraints on a solution | $2.71{ }_{\text {A-D }}, 2.72_{\text {B-E }}$ |
| 1c | - Probing pursuit: invent, evaluate, and execute probing-actions | $2.71_{\mathrm{B}, \mathrm{D}}, 2.72_{\mathrm{F}}$ |
| 2a | SELECT an old theory (observations + retroductive logic + ...) | 2.51 |
| 2b | INVENT a new theory (observations + retroductive logic + ...) | 2.52-2.53 |
| 3a | DESIGN EXPERIMENT <br> (find gaps, do thought experiments,...) | $2.61-2.62,2.63 \mathrm{~A}$ |
| 3b | DO EXPERIMENT, make OBSERVATIONS | 2.11 E |
| 4a | theories + system $\rightarrow$ PREDICTION (using "if-then" deductive logic) | $2.11_{\text {D }}, 2.11_{\text {B-C }}$ |
| 4b | estimate degree-of-AGREEMENT, by comparing obs with T-predictions | $2.12 \mathrm{~A}, 2.52$ |
| 4 c | estimate degree-of-CONTRAST, compare obs-vs-predn for T \& alt-Ts | $2.12_{\text {B }}, 2.61_{\mathrm{F}}$ |
| 4d | PREVIOUS agreement-and-contrast (empirical evaltn for previous expmts) | $2.12 \mathrm{C}, 2.52 \mathrm{E}$ |
| 5a | INTERNAL characteristics of Theory (check T's ontology, systematicity,...) | 2.21-2.26 |
| 5b | EXTERNAL relations with other Ts (domain overlap, shared components) | 2.27-2.28 |
| 6 a | metaphysical \& ideological | 2.31 B |
| 6b | psychological, practical, authority | $2.31 \mathrm{~A}, \mathrm{C}$ |
| 7 a | EVALUATION $\rightarrow$ "conclusion" $\Delta$ in T-status? retain revise reject | 2.42 |
| 7b | - Persuasion (of self, research group, or outsiders) | $2.61{ }_{\mathrm{G}}, 2.71_{\mathrm{E}}, 2.72_{\mathrm{C}, \mathrm{F}}$ |

abbreviations: obs = observations, $\mathrm{T}=$ theory, predn $=$ prediction, alt $=$ alternative, evaltn $=$ evaluation, expmts $=$ experiments,
$\Delta=$ change

Table 3: Science Experiences during the "Black Box Model Revising" activities

|  | $\mathbf{3 . 3 1} \mathrm{A}$ <br> Black Box model-building | 3.31B <br> Black Box conference | $\mathbf{3 . 3 1}_{\mathrm{C}}$ <br> Black Box model-revising |
| :---: | :---: | :---: | :---: |
| - Preparation for content, process; backward-reaching, forward-reaching | backward, NO ? forward. YES | forward: listen to others' ideas | backward: yes <br> forward: ves |
| - Posing of an area to study, and of constraints on a | NO (area) yes (constraints) | $\mathrm{NO}$ yes | $\mathrm{NO}$ <br> yes |
| - Probing pursuit: invent, evaluate, and execute probing-actions | YES ! <br> manvdecicions | YES <br> for persuasion | YES |
| SELECT an old theory (observations + retroductive logic + ...) | yes, but old Ts are not sufficient | own model from first day | begin w own T or out-group T |
| INVENT a new theory (observations + retroductive logic + ...) | T-building and T-revision | is possible but is not expected | by revision of existing theory |
| DESIGN EXPERIMENT <br> (find gaps, do thought experiments....) | yes; eventually is guided by T | to support own or to challenge | yes |
| DO EXPERIMENT, make OBSERVATIONS | yes | to demonstrate, | yes |
| theories + system $\rightarrow$ PREDICTION (using "if-then" deductive logic) | usually done after experiment | as explanation, or as | yes |
| estimate degree-of-AGREEMENT, by comparing obs with T-predictions | yes | yes, this is important | yes |
| estimate degree-of-CONTRAST, compare obs-vs-predn for T \& alt-Ts | competitive Ts of own group | compare own T with other | yes |
| PREVIOUS agreement-and-contrast (empirical evaltn for previous expmts) | as experiments accumulate | yes, all data is considered | yes, from <br> all 3 days |
| INTERNAL characteristics of Theory (check T's ontology, svstematicity....) | ask "Is it possible?" | yes | yes |
| EXTERNAL relations with other Ts (domain overlap, shared components) | check w known physical laws | yes | yes |
| metaphysical \& ideological | assumption of consistency | consistency | yes |
| psychological, practical, authority | relations with own group, Sue | relations w all students \& Sue | yes |
| EVALUATION $\rightarrow$ "conclusion" <br> $\Delta$ in T-status? retain revise reject | yes, through whole process | of own T and other Ts | to decide on a "final model" |
| - Persuasion <br> (of self, research group, or outsiders) | persuasion of self \& groupers | persuasion of others, mainly | yes |

abbreviations: obs = observations, $\mathrm{T}=$ theory, predn $=$ prediction, alt $=$ alternative, evaltn $=$ evaluation, expmts $=$ experiments, $\Delta=$ change; $\mathrm{w}=$ with

Table 4: Science Experiences during the "Genetics Phenomena" activities

|  | $3.32_{\mathrm{A}}$ <br> cookie analogy | $3.32_{\mathrm{B}}$ <br> human variations | $3.32_{C}$ <br> human pedigrees |
| :---: | :---: | :---: | :---: |
| - Preparation for content, process; backward-reaching, forward-reaching | learn concepts and terms | learn concepts and terms | learn concepts and terms |
| - Posing of an area to study, and of constraints on a solution | yes (questions) | yes (questions) | yes (questions) |
| - Probing pursuit: invent, evaluate, and execute probing-actions | - | - | whether to interpret |
| SELECT an old theory (observations + retroductive logic + ...) | - | - | - |
| INVENT a new theory (observations + retroductive logic + ...) | - | - | finding patterns in the data |
| DESIGN EXPERIMENT <br> (find gaps, do thought experiments,...) | variations on a basic recipe | - | - |
| DO EXPERIMENT, make OBSERVATIONS | bake cookies, examine them | make observations | (second-hand data is used) |
| theories + system $\rightarrow$ PREDICTION (using "if-then" deductive logic) | - | - | - |
| estimate degree-of-AGREEMENT, by comparing obs with T-predictions | - | - | - |
| estimate degree-of-CONTRAST, compare obs-vs-predn for T \& alt-Ts | - | - | - |
| PREVIOUS agreement-and-contrast (empirical evaltn for previous expmts) | - | - | - |
| INTERNAL characteristics of Theory (check T's ontology, systematicity,...) | - | - | - |
| EXTERNAL relations with other Ts (domain overlap, shared components) | - | - | - |
| metaphysical \& ideological | - | - | - |
| psychological, practical, authority | class bonding: milk \& cookies! | more bonding | - |
| EVALUATION $\rightarrow$ "conclusion" $\Delta$ in T-status? retain revise reject delay | - | - | - |
| - Persuasion (of self, research group, or outsiders) | - | - | - |

abbreviations: obs = observations, $\mathrm{T}=$ theory, predn = prediction, alt $=$ alternative, evaltn $=$ evaluation, expmts $=$ experiments, $\Delta=$ change $; \mathrm{w}=$ with

Table 5: Science Experiences during the "Initial Models" activities

|  | $\mathbf{3 . 3 3}_{\mathrm{A}}$ <br> building a model of dominance | $\mathbf{3 . 3 3}_{\mathrm{B}}$ <br> building a model of meiosis | $\mathbf{3 . 3 3}_{\mathrm{C}}$ <br> GCK <br> practicing and exam |
| :---: | :---: | :---: | :---: |
| - Preparation for content, process; backward-reaching, forward-reaching | preparation for model revising | preparation for model revising | preparation for model revising |
| - Posing of an area to study, and $\qquad$ | $\begin{aligned} & \text { NO } \\ & \text { yes } \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { NO } \\ & \text { yes } \end{aligned}$ | $\begin{aligned} & \text { NO } \\ & \text { ves } \\ & \hline \end{aligned}$ |
| - Probing pursuit: invent, evaluate, and execute probing-actions | minimal choices about | minimal choices about | yes, students decide actions |
| SELECT an old theory (observations + retroductive logic + ...) | assumed to be not available | mitosis; but it is not adequate | yes, but there is only one option |
| INVENT a new theory (observations + retroductive logic + ...) | yes, by guided construction | yes, by guided construction | retroduction only for system |
| DESIGN EXPERIMENT <br> (find gaps, do thought experiments....) | watch how an expert does it | field study? <br> ves | yes, but within narrow limits |
| DO EXPERIMENT, make OBSERVATIONS | peas provided; classify \& | field exprmts $\rightarrow$ observations | yes |
| theories + system $\rightarrow$ PREDICTION (using "if-then" deductive logic) | yes | yes | yes |
| estimate degree-of-AGREEMENT, by comparing obs with T-predictions | major factor in development | major factor in development | yes (no anomalies) |
| estimate degree-of-CONTRAST, compare obs-vs-predn for T \& alt-Ts | "blending" T is a competitor | mitotic model is a competitor | not possible: no alternative |
| PREVIOUS agreement-and-contrast (empirical evaltn for previous expmts) | yes | yes | yes |
| INTERNAL characteristics of Theory (check T's ontology, systematicity....) | yes <br> in Mendel | yes | understanding |
| EXTERNAL relations with other Ts (domain overlap, shared components) | this is not a major factor vet | yes; relations with | no; has been done already |
| metaphysical \& ideological | assumption of consistency | consistency | sophisticated "consistency" |
| psychological, practical, authority | collaborations <br> w Mendel.... | collaboration w group \& class | social w group and w teacher |
| EVALUATION $\rightarrow$ "conclusion" <br> $\Delta$ in T-status? retain revise reject | accept Mendel's model | accept meiotic model | no reason not to retain |
| - PerRUASION <br> (of self, research group, or outsiders) | by empirical + authorities... | by empirical + conceptual $+\ldots$ | re: exp-system, using GCK.... |

abbreviations: obs = observations, $\mathrm{T}=$ theory, $\operatorname{predn}=$ prediction, alt $=$ alternative, evaltn = evaluation, expmts $=$ experiments, $\Delta=$ change; $\mathrm{w}=$ with, $\exp =\operatorname{experimental}$

Table 6: Science Experiences during the "Genetics Model Revising" activities

|  | $\begin{gathered} \mathbf{3 . 3 4}_{\mathrm{A}} \text { : } \\ \text { revising the } \\ \text { existing model(s) } \end{gathered}$ | $\mathbf{3 . 3 4}_{\mathbf{B}}:$ <br> conference to discuss models that are invented |
| :---: | :---: | :---: |
| - Preparation for content, process; backward-reaching, forward-reaching | all preceding activities are to prepare for this | GCK work is a preparation for this |
| - Posing of an area to study, and $\qquad$ | $\begin{gathered} \mathrm{NO} \\ \text { ves } \end{gathered}$ | NO <br> ves (goal is persuasion) |
| - Probing pursuit: invent, evaluate, $\qquad$ | YES, many decisions about pursuit-actions | preliminary planning and quick improvisation |
| SELECT an old theory (observations + retroductive logic + ...) | in Round 1, no options; later, students can choose | as starting point to show how new T was |
| INVENT a new theory (observations + retroductive logic $+\ldots$..) | this is the focal point of the entire course: YES | presented model usually does not need revising |
| DESIGN EXPERIMENT <br> (find gaps, do thought experiments....) | students can only decide which parents to cross | for own presentation, or to challenge others |
| DO EXPERIMENT, make OBSERVATIONS | GCK provides data, students observe \& use it | planned by presenters, or due to challenge |
| theories + system $\rightarrow$ PREDICTION (using "if-then" deductive logic) | for old or new Ts, to explain or predict | prediction must be done BEFORE an experiment |
| estimate degree-of-AGREEMENT, by comparing obs with T-predictions | this is usually the major factor in T-evaluation | this is most important factor in persuasion |
| estimate degree-of-CONTRAST, compare obs-vs-predn for T \& alt-Ts | students can recognize "crucial experiments" | if needed to compare competitive models |
| PREVIOUS agreement-and-contrast (empirical evaltn for previous expmts) | all data is considered | yes |
| INTERNAL characteristics of Theory (check T's ontology, systematicity....) | yes | yes |
| EXTERNAL relations with other Ts (domain overlap, shared components) | yes | yes |
| metaphysical \& ideological | consistency expected, if sophistication \& patience | consistency |
| psychological, practical, authority | social interactions; also practical + authority | w students inside and outside group, and Sue |
| EVALUATION $\rightarrow$ "conclusion" <br> $\Delta$ in T-status? retain revise reject delay | reject old model(s), maybe accept new model | reject the old model? accept the new model? |
| - Persualion <br> (of self, research group, or outsiders) | yes, at several levels | external persuasion is now the main event |

abbreviations: obs = observations, $\mathrm{T}=$ theory, predn $=$ prediction, alt $=$ alternative, evaltn = evaluation, expmts $=$ experiments, $\Delta=$ change; $w=$ with

Table 7: Science Experiences during the "Manuscript Preparation" activities

|  | 3.35 |
| :---: | :---: |
| Manuscript Writing and Manuscript Revising |  |$|$

abbreviations: obs = observations, $\mathrm{T}=$ theory, predn = prediction, alt $=$ alternative, evaltn $=$ evaluation, expmts $=$ experiments, $\Delta=$ change

## Table 8: Functional Relationships between and within Instructional Activities

note: This table, with the page in "landscape" orientation
so you can see the entire table, is in another PDF-file.

|  | $3.31 \mathrm{AC}$ <br> Black Box model | $3.31_{B}$ <br> Black Box con- | $3.32 \mathrm{AB}$ <br> cookies variations pedigrees | $3.33 \mathrm{~A}$ <br> construct Mendel model | $3.33_{\mathrm{B}}$ <br> construct meioticm odel | $3.33 \mathrm{C}$ <br> GCK with no revising | $\begin{gathered} 3.34 \mathrm{~A} \\ \text { GCK } \\ \text { model } \\ \text { revising } \end{gathered}$ | $\begin{gathered} 3.34 \mathrm{~B} \\ \text { GCK } \\ \text { con- } \\ \text { ference } \end{gathered}$ | $3.35$ <br> manuscript |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| sackward preparation | none | model revising |  |  |  |  | all prior activities | model revising | model revising |
| forward preparation | process |  | content | content process | content process | content GCK | for persuasion |  |  |
| Posing | no, yes |  |  |  |  |  | no, yes |  | yes, yes |
| Probing for PSolving | YES ! | prsuasn |  | guided | guided |  | YES ! | prsuasn | prsuasn |
| Model Selection | old M |  |  |  | mitosis |  | old Ms |  |  |
| Model Invention | MODEL |  |  | model | model | - | MODEL | for |  |
| Expmtal Design | physical | for |  |  |  |  | limited | for | for |
| Expmt \& Obs | expmt |  | obs | obs | remember | mental | MENTAL |  |  |
| Prediction | w new | pre-dict |  |  |  |  | w new | pre-dict |  |
| Agreement | main | main |  | main | main | agreement | main | main | main |
| Predictive Contrast | criterion | argument |  | criterion | criterion | no alt-Ms | criterion | argument | argument |
| Previous Expmts |  |  |  |  |  |  |  |  |  |
| Internal Consistency |  |  |  |  |  |  |  |  |  |
| External Consistency | with laws |  |  |  |  |  | w old Ms |  |  |
| Metaphysical |  |  |  |  |  | cnsstcy |  |  |  |
| Personal / Authority |  |  | bonding |  |  |  |  |  |  |
| Conclusion | by group | by others |  | as class | as class |  | by group | by others | by others |
| Persuasion | in group | external |  | by tchr | by tchr |  | in group | external | external |

abbreviations: prsuasn = persuasion, $\mathrm{M}=$ model, $\mathrm{MB}=$ Mendel's Bible, expmt = experiment, obs = observation, alt $=$ alternative,
cnsstcy $=$ consistency, motivn $=$ motivation, tchr $=$ teacher

Figure 15: an external representation for a model of simple dominance.

OView 0-A: theory for dominance

Punnet Squares (for genotypes) and phenotypes

|  | $\begin{gathered} \text { aa } \\ \text { A } \end{gathered}$ | $\begin{gathered} \text { ab } \\ \text { A } \end{gathered}$ | $\begin{gathered} \text { bb } \\ \text { B } \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| aa | aa aa aa aa | aa ab aa ab | ab ab $a b a b$ |
| A | $\begin{array}{ll} \mathrm{A} & \mathrm{~A} \\ \mathrm{~A} & \mathrm{~A} \\ \hline \end{array}$ | $\begin{array}{ll}  & \text { A } \\ \text { A } & \text { A } \end{array}$ | $\begin{array}{ll} A & A \\ A & A \end{array}$ |
| ab | aa aa ba ba | aa ab ba bb | ab ab bb bb |
| A | $\begin{array}{ll} \mathrm{A} & \mathrm{~A} \\ \mathrm{~A} & \mathrm{~A} \end{array}$ | $\begin{array}{ll} \mathrm{A} & \mathrm{~A} \\ \mathrm{~A} & \mathrm{~B} \end{array}$ | $\begin{array}{ll}  & \text { A } \\ \text { B } & \text { B } \end{array}$ |
| bb | ba ba ba ba | ba bb ba bb | bb bb bb bb |
| B | $\begin{array}{ll} A & A \\ A & A \end{array}$ | $\begin{array}{ll} \text { A } & \text { B } \\ \text { A } & \text { B } \end{array}$ | $\begin{array}{ll} B & B \\ B & B \end{array}$ |

OView 0-B: statistics for phenotypes

OView 0-C: the 6 "cross
OView 0-C: the 6 "cross
possibilities"

|  | $\mathbf{a a}$ <br> A | $\mathbf{a b}$ <br> A | $\mathbf{b b}$ <br> B |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{a a}$ <br> A | $100 \%$ | A | $100 \%$ | A | $100 \%$ | A.


|  | aa <br> A | $\mathbf{a b}$ <br> A | $\mathbf{b b}$ <br> B |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{a a}$ <br> A | $100 \% \mathrm{~A}$ | $100 \%$ | A | $100 \%$ | A.

OView 0-D:
theory-predicted data for dominance

|  | father <br> A | father <br> B |
| :---: | :---: | :---: |
| $\begin{gathered} \text { mother } \\ \text { A } \end{gathered}$ | $\begin{gathered} 100 \% \mathrm{~A} \\ \text { or } \end{gathered}$ | $\begin{gathered} 100 \% \mathrm{~A} \\ \text { or } \end{gathered}$ |
|  | 75\% A | 50\% A |
|  | 25\% B | 50\% B |
| $\begin{gathered} \text { mother } \\ \text { B } \end{gathered}$ | 100\% A | 100\% B |
|  | or |  |
|  | 50\% A |  |
|  | 50\% B |  |

Figure 16: Data and Theory for codominance in Round 1

OView 1-A: data and anomalies

|  | C | D | E |  |
| :---: | :---: | :---: | :---: | :---: |
| C | 100\% C | 50\% C | 100\% D |  |
|  |  | 50\% D |  |  |
| D | 50\% C | 25\% |  |  |
|  | 50\% D | 50\% | 50\% |  |
|  |  | 25\% E | 50\% |  |
| E | 100\% D | 50\% D |  |  |
|  |  | 50\% E | 100\% |  |

In addition, there are "missing results";
DxD never produces $100 \% \mathrm{D}$, and
no 'like with like' cross (CxC, DxD, ExE) ever produces a 75-25 mix.

OView 1-B: theory for codominance

|  | $\begin{gathered} \mathbf{c c} \\ \mathrm{C} \end{gathered}$ | $\begin{gathered} \mathbf{c e} \\ \mathrm{D} \end{gathered}$ | $\begin{gathered} \text { ee } \\ \mathrm{E} \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| cc | CC CC CC Cc | Cc ce CC ce | ce ce ce ce |
| C | $\begin{array}{ll} \mathrm{C} & \mathrm{C} \\ \mathrm{C} & \mathrm{C} \end{array}$ | $\begin{array}{ll} C & D \\ C & D \end{array}$ | $\begin{array}{ll} D & D \\ D & D \end{array}$ |
| ce | CC Cc ec ec | Cc ce ec ee | ce ce ee ee |
| D | $\begin{array}{ll} C & C \\ D & D \\ \hline \end{array}$ | $\begin{array}{ll} C & D \\ D & E \end{array}$ | $\begin{array}{ll} \text { D } & \text { D } \\ \text { E } & \text { E } \end{array}$ |
| ee | ec ec ec ec | ec ee ec ee | ee ee ee ee |
| E | $\begin{array}{ll} \mathrm{D} & \mathrm{D} \\ \mathrm{D} & \mathrm{D} \\ \hline \end{array}$ | $\begin{array}{ll} \text { D } & \text { E } \\ \text { D } & \text { E } \\ \hline \end{array}$ | $\begin{array}{ll}\text { E } & \mathrm{E} \\ \mathrm{E} & \mathrm{E}\end{array}$ |

OView 1-C: statistics for phenotypes

|  | cc | ce | ee |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | C | D | E |  |  |  |
| $\mathbf{c c}$ | $100 \%$ | C | $50 \%$ | C |  |  |
| C |  | $50 \%$ | D | $100 \%$ | D |  |
|  |  |  |  |  |  |  |
| $\mathbf{c e}$ | $50 \%$ | C | $25 \%$ | C |  |  |
| D | $50 \%$ | D | $50 \%$ | D | $50 \%$ | D |
|  |  | $25 \%$ | E | $50 \%$ | E |  |
| $\mathbf{e e}$ |  |  |  |  |  |  |
| E | $100 \%$ | D | $50 \%$ | D |  |  |

Figure 17: Data and Theory for multiple alleles in Round 2

OView 2-B: data for codominance
OView 2-A: data for dominance

|  | A | B |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $100 \%$ | A | $100 \%$ | A |
| A | or | or |  |  |
|  | $75 \%$ | A | $50 \%$ | A |
|  | $25 \%$ | B | $50 \%$ | B |
|  | $100 \%$ | A |  |  |
| B | or |  |  |  |
|  | $50 \%$ | A | $100 \%$ | B |
|  | $50 \%$ | B |  |  |
|  |  |  |  |  |


|  | $\mathbf{c c}$ | $\mathbf{c e}$ | $\mathbf{e e}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | C | D | E |  |  |
| $\mathbf{c c}$ | $100 \%$ | C | $50 \%$ | C |  |
| C |  | $50 \%$ | D | $100 \%$ | D |
|  |  |  |  |  |  |
| $\mathbf{c e}$ | $50 \%$ | C | $25 \%$ | C |  |
| D | $50 \%$ | D | $50 \%$ | D | $50 \%$ |
|  |  |  | D |  |  |
|  | $25 \%$ | E | $50 \%$ | E |  |
| $\mathbf{e e}$ |  |  |  |  |  |
| E | $100 \%$ | D | $50 \%$ | D |  |
|  |  | $50 \%$ | E | $100 \%$ | E |

OView 2-C: data for multiple alleles, and clues for anomaly resolution

|  | R | 0 | S | T |
| :---: | :---: | :---: | :---: | :---: |
| R | 100\% R | 50\% R | 100\% 0 | 100\% R |
|  | or | 50\% O | or | or |
|  | 75\% R | or | 50\% R | 50\% R |
|  | 25\% T | 50\% R | 50\% O | 50\% T |
|  |  | 25\% O | or |  |
|  |  | 25\% S | 50\% O |  |
|  |  |  | 50\% S |  |
|  |  |  | or |  |
|  |  |  | 25\% R |  |
|  |  |  | 25\% O |  |
|  |  |  | 25\% S |  |
| 0 |  |  | 25\% |  |
|  |  | 25\% R | 25\% R | 50\% R |
|  |  | 50\% O | 25\% O | 50\% S |
|  |  | 25\% S | 50\% S |  |
|  |  |  | or |  |
|  |  |  | 50\% O |  |
|  |  |  | 50\% S |  |
| S |  |  | 100\% S | 100\% S |
|  |  |  | or | or |
|  |  |  | 75\% S | 50\% S |
|  |  |  | 25\% T | 50\% T |
| T |  |  |  | 100\% T |

Figure 17 (continued)

OView 2-D: theory for multiple alleles

|  | $\begin{gathered} \text { rr } \\ \text { R } \end{gathered}$ | $\begin{gathered} r t \\ R \end{gathered}$ | $\begin{gathered} \text { rs } \\ 0 \end{gathered}$ | $\begin{gathered} \text { Ss } \\ \text { S } \end{gathered}$ | $\begin{gathered} \text { st } \\ \text { s } \end{gathered}$ | $\begin{gathered} \mathrm{tt} \\ \mathrm{~T} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| rr | rr rr | rr rt | rr rs | rs rs | rs rt | rt rt |
| R | rr rr | rr rt | rr rs | rs rs | rs rt | rt rt |
| rt |  | rr rt | rr rs | rs rs | rs rt | rt rt |
| R |  | tr tt | tr ts | ts ts | ts tt | tt tt |
| rs |  |  | rr rs | rs rs | rs rt | rt rt |
| 0 |  |  | sr SS | SS SS | ss st | st st |
| ss |  |  |  | SS SS | ss st | st st |
| S |  |  |  | SS SS | ss st | st st |
| st |  |  |  |  | ss st | st st |
| S |  |  |  |  | ts tt | tt tt |
| tt |  |  |  |  |  | tt tt |
| T |  |  |  |  |  | tt tt |

OView 2-E: phenotypes for one codominance, "t loses"

|  | $\begin{gathered} \mathrm{rr} \\ \mathrm{R} \\ \hline \end{gathered}$ | $\begin{gathered} \mathrm{rt} \\ \mathrm{R} \\ \hline \end{gathered}$ | $\begin{gathered} \text { rs } \\ 0 \end{gathered}$ | $\begin{gathered} \text { ss } \\ \text { S } \end{gathered}$ | $\begin{gathered} \text { st } \\ \text { S } \end{gathered}$ | $\begin{gathered} \mathrm{tt} \\ \mathrm{~T} \end{gathered}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| rr | R R | R R | R O | 0 |  |  | R |
| R | R R | R R | R O | 0 | 0 R |  | R |
| rt |  | R R |  |  | 0 | R | R |
| R |  | R T | R S | S | S | T | T |
| rs |  |  | R O | 0 | 0 | R | R |
| 0 |  |  | 0 S |  | S | S | S |
| ss |  |  |  |  |  | S | S |
| S |  |  |  |  |  |  | S |
| st |  |  |  |  | S | S | S |
| S |  |  |  |  |  |  | T |
| T |  |  |  |  |  |  |  |
| T |  |  |  |  |  |  |  |

OView 2-F: the 7 types of inhritance sub-patterns for 3 alleles

|  | 3 varns | 3 varns | 4 varns | 4 varns | 4 varns | 5 varns | 6 varns |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | dominance <br> hierarchica <br> 1 | dominance <br> $\mathrm{r}-\mathrm{p}-\mathrm{s}$ | codominance <br> t wins | codominance <br> t loses | codominance <br> t splits | codominance <br> for 2 of 3 | codominance <br> for 3 of 3 |
| rr | R | R | R | $\mathbf{R}$ | R | R | R |
| ss | S | S | S | $\mathbf{S}$ | S | S | S |
| tt | T | T | T | $\mathbf{T}$ | T | T | T |
| rs | R | R | RS | $\mathbf{R S}$ | RS | RS | RS |
| st | S | S | T | $\mathbf{S}$ | S | ST | ST |
| rt | R | T | T | $\mathbf{R}$ | T | R | RT |

Figure 18: Data and Theory for sex linkage in Round 3

OView 3-A: ratios for all offspring, anomalies w.r.t. dominance

|  | H | Z |
| :---: | :---: | :---: |
|  | $100 \% \mathrm{H}$ | $100 \% \mathrm{H}$ |
| H | or | or |
|  | $75 \% \mathrm{H}$ | $50 \% \mathrm{H}$ |
|  | $25 \% \mathrm{Z}$ | $50 \% \mathrm{Z}$ |
|  | $50 \% \mathrm{H}$ | $100 \% \mathrm{Z}$ |
| Z | $50 \% \mathrm{Z}$ |  |
|  | but not |  |
|  | $100 \% \mathrm{H}$ |  |

OView 3-B: ratios for females \& males; anomalies w.r.t. dominance

|  | H | Z |
| :---: | :---: | :---: |
|  | $100 \% \mathrm{Hf}$ | $100 \% \mathrm{Hf}$ |
|  | $100 \% \mathrm{Hm}$ | $100 \% \mathrm{Hm}$ |
|  | Or | Or |
|  | $100 \% \mathrm{Hf}$ | $50 \% \mathrm{Hf}$ |
|  | $0 \% \mathrm{Zf}$ | $50 \% \mathrm{Zf}$ |
|  | $50 \% \mathrm{Hm}$ | $50 \% \mathrm{Hm}$ |
|  | $50 \% \mathrm{Zm}$ | $50 \% \mathrm{Zm}$ |
| Z | $100 \% \mathrm{Hf}$ | $100 \% \mathrm{Zf}$ |
|  | $100 \% \mathrm{Zm}$ | $100 \% \mathrm{Zm}$ |

OView 3-C: theory for dominance

|  | $\begin{gathered} \mathbf{h h} \\ \mathrm{H} \end{gathered}$ | $\begin{gathered} \mathbf{h z} \\ \mathrm{H} \end{gathered}$ | $\begin{gathered} \mathbf{z ~ z} \\ \text { Z } \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| hh | hh hh | hh hz | hz hz |
|  | hh hh | hh hz | hz hz |
| H | H H | H H | H H |
|  | H H | H H | H H |
| hz | hh hh | hh hz | hz hz |
|  | zh zh | zh zz | zz zz |
| H | H H | H H | H H |
|  | H H | H Z | Z Z |
| zz | zh zh | zh zz | zz zz |
|  | zh zh | zh zz | zz zz |
| Z | H H | H Z | Z Z |
|  | H H | H Z | Z |

OView 3-D: theory for sex-linkage

|  | h- | $\begin{gathered} \mathrm{z}- \\ \mathrm{Z} \end{gathered}$ |
| :---: | :---: | :---: |
| hh | hh h- | hz h- |
|  | hh h- | hz h- |
| H | Hf Hm | Hf Hm |
|  | Hf Hm | Hf Hm |
| hz | hh h- | hz h- |
|  | zh z- | zz z- |
| H | Hf Hm | Hf Hm |
|  | Hf Zm | Zf Zm |
| zz | zh z- | zz z- |
|  | $\mathrm{zh} \mathrm{z-}$ | zz z- |
| Z | Hf Zm | Zf Zm |
|  | Hf Zm | Zf Zm |

Figure 19: Data and Theory for autosomal linkage in Round 4

OView 4-A: Punnett Squares for the same phenotype-cross (AI x AI), using two different genotype-crosses: "aaii x aaii" on the left side, "abin x abin" on the right side.


|  |  | $\begin{aligned} & \text { AI } \\ & \text { (ab } \\ & \text { in) } \end{aligned}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | ai | an | bi | bn |
|  | ai | $\begin{gathered} \text { aa ii } \\ \text { AI } \end{gathered}$ | $\begin{gathered} \text { aa in } \\ \text { AI } \end{gathered}$ | $\begin{gathered} \mathrm{ab} \text { ii } \\ \text { AI } \end{gathered}$ | ab in AI |
| AI | an | $\begin{gathered} \text { aani } \\ \text { AI } \end{gathered}$ | $\begin{gathered} \text { aa nn } \\ \text { AN } \end{gathered}$ | $\begin{gathered} \mathrm{ab} \mathrm{ni} \\ \mathrm{AI} \end{gathered}$ | $a b \mathrm{nn}$ AN |
| (ab in) |  | $\begin{gathered} \text { ba ii } \\ \text { AI } \end{gathered}$ | $\begin{gathered} \hline \mathrm{ba} \text { in } \\ \mathrm{AI} \\ \hline \end{gathered}$ | bb ii BI | bb in BI |
|  |  | $\begin{gathered} \hline \text { ba ni } \\ \text { AI } \end{gathered}$ | $\begin{gathered} \text { ba nn } \\ \text { AN } \end{gathered}$ | bb ni BI | bb nn BN |

ratio ( $\mathrm{AI}: \mathrm{AN}: \mathrm{BI}: \mathrm{BN}$ )
is 9:3:3:1

OView 4-B: Phenotype data, predicted using Punnett Squares, for all genotype combinations.
Data shows ratios for AI:AN:BI:BN. For example, for AIxAI one of the 16 cells is "6200" to show the 6:2:0:0 ratio, with $75 \% \mathrm{AI}, 25 \% \mathrm{AN}, 0 \% \mathrm{BI}$, and $0 \% \mathrm{BN}$.
The shaded cells are predictions that, with linkage, do not match observations.

|  |  | AI <br> aa <br> ii | AI <br> aa <br> in | AI <br> ab <br> ii | $\begin{aligned} & \text { AI } \\ & \text { ab } \\ & \text { in } \end{aligned}$ | AN <br> aa <br> nn | AN <br> ab <br> nn | BI <br> bb <br> ii | $\begin{aligned} & \text { BI } \\ & \text { bb } \\ & \text { in } \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | aa ii | 8000 | 8000 | 8000 | 8000 | 8000 | 8000 | 8000 | 8000 | 8000 |
| AI | aa in | 8000 | 6200 | 8000 | 6200 | 4400 | 4400 | 8000 | 6200 | 4400 |
| AI | ab ii | 8000 | 8000 | 6020 | 6020 | 8000 | 6020 | 4040 | 4040 | 4040 |
| AI | ab in | 8000 | 6200 | 6020 | 9331 | 4400 | 3311 | 4040 | 3131 | 2222 |
| AN | aa nn | 8000 | 4400 | 8000 | 4400 | 0800 | 0800 | 8000 | 4400 | 0800 |
| AN | ab nn | 8000 | 4400 | 6020 | 3311 | 0800 | 0602 | 4040 | 2222 | 0404 |
| BI | bb ii | 8000 | 8000 | 4040 | 4040 | 8000 | 4040 | 0080 | 0080 | 0080 |
| BI | bb in | 8000 | 6200 | 4040 | 3131 | 4400 | 2222 | 0080 | 0062 | 0044 |
| BN | bb nn | 8000 | 4400 | 4040 | 2222 | 0800 | 0404 | 0080 | 0044 | 0008 |

OView 4-C: Punnett Squares, if there is autosomal linkage, for the four anomalous crosses. The bold numbers show the phenotype ratios for each area; non-bold numbers show the ratios that occur if there is no linkage, when all cells are combined.




OView 4-D: Dominance with autosomal linkage; an explanation for anomalies in OView 4D. The shading shows parental genotypes that produce different gametes if there is linkage, and the cross-results that (as shown in OView 4-D) are anomalous.

|  | AI <br> aa <br> ii | AI <br> aa <br> in | AI <br> ab <br> ii | AI <br> ab <br> in | AI <br> ab <br> in | AN <br> aa <br> nn | AN <br> ab <br> nn | $\begin{aligned} & \mathrm{BI} \\ & \mathrm{bb} \\ & \mathrm{ii} \end{aligned}$ | BI <br> bb <br> in | BN <br> bb <br> nn |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ai <br> ai | $\begin{aligned} & \text { ai } \\ & \text { an } \end{aligned}$ | $\begin{aligned} & \text { ai } \\ & \text { bi } \end{aligned}$ | $\begin{aligned} & \mathrm{ai} \\ & \mathrm{bn} \end{aligned}$ | an bi | $\begin{aligned} & \text { an } \\ & \text { an } \end{aligned}$ | $\begin{aligned} & \text { an } \\ & \text { bn } \end{aligned}$ | $\begin{aligned} & \mathrm{bi} \\ & \mathrm{bi} \end{aligned}$ | $\begin{aligned} & \mathrm{bi} \\ & \text { bn } \end{aligned}$ | $\begin{aligned} & \text { bn } \\ & \text { bn } \end{aligned}$ |
| $\begin{aligned} & \hline \text { ai } \\ & \text { ai } \\ & \hline \end{aligned}$ | 8000 | 8000 | 8000 | 8000 | 8000 | 8000 | 8000 | 8000 | 8000 | 8000 |
| $\begin{aligned} & \text { ai } \\ & \text { an } \end{aligned}$ | 8000 | 6200 | 8000 | 6200 | 6200 | 4400 | 4400 | 8000 | 6200 | 4400 |
| $\begin{aligned} & \text { ai } \\ & \text { bi } \end{aligned}$ | 8000 | 8000 | 6020 | 6020 | 6020 | 8000 | 6020 | 4040 | 4040 | 4040 |
| $\begin{aligned} & \text { ai } \\ & \text { bn } \end{aligned}$ | 8000 | 6200 | 6020 | 6002 | 4220 | 4400 | 4202 | 4040 | 4022 | 4004 |
| $\begin{aligned} & \mathrm{an} \\ & \mathrm{bi} \\ & \hline \end{aligned}$ | 8000 | 6200 | 6020 | 4220 | 4220 | 4400 | 2420 | 4040 | 2240 | 0440 |
| an | 8000 | 4400 | 8000 | 4400 | 4400 | 0800 | 0800 | 8000 | 4400 | 0800 |
| $\begin{aligned} & \hline \text { an } \\ & \text { bn } \end{aligned}$ | 8000 | 4400 | 6020 | 4202 | 2420 | 0800 | 0602 | 4040 | 2222 | 0404 |
| $\begin{aligned} & \hline \mathrm{bi} \\ & \mathrm{bi} \\ & \hline \end{aligned}$ | 8000 | 8000 | 4040 | 4040 | 4040 | 8000 | 4040 | 0080 | 0080 | 0080 |
| $\begin{aligned} & \hline \mathrm{bi} \\ & \mathrm{bn} \end{aligned}$ | 8000 | 6200 | 4040 | 4022 | 2240 | 4400 | 2222 | 0080 | 0062 | 0044 |
| $\begin{aligned} & \mathrm{bn} \\ & \mathrm{bn} \\ & \hline \end{aligned}$ | 8000 | 4400 | 4040 | 4004 | 0440 | 0800 | 0404 | 0080 | 0044 | 0008 |

OView 4-E: This shows why the results with no linkage (on the left, as in OView 4-A) are the same as the overall results with linkage (on the right, as in OView 4-C). 4 of 16 results (in 4-A) can occur with the "\#1" set of linked parents (in 4-C); the other 12 results (in 4-A) occur with the other three parental crosses in 4-C.

| ( ab in) |  |  |  |  | ( ab in) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ai | an | bi | bn |  |  | ai | bn | an | bi |
| ai | aa ii | aa in | ab ii | ab in |  | ai | aa | ab | aa | ab |
|  | \#1 | 2 | 2 | \#1 |  |  | ii | in | in | ii |
| a an | aa ni | aa nn | ab ni | ab nn |  |  | \#1 | \#1 | 2 | 2 |
| b | 3 | 4 | 4 | 3 | a | bn | ba | bb | ba | bb |
| i bi | ba ii | ba in | bb ii | bb in | b |  | ni | nn | nn | ni |
| n | 3 | 4 | 4 | 3 |  |  | \#1 | \#1 | 2 | 2 |
| bn | ba ni | ba nn | bb ni | bb nn | i | an | aa | ab | aa | ab |
|  | \#1 | 2 | 2 | \#1 | n |  | ni | nn | nn | ni |
|  |  |  |  |  |  |  | 3 | 3 | 4 | 4 |
|  |  |  |  |  |  | bi | ba | bb | ba | bb |
|  |  |  |  |  |  |  | ii | in | in | ii |
|  |  |  |  |  |  |  | 3 | 3 | 4 | 4 |

OView 4-F: Comparing predictions (from 4-A or 4-B) with observations (from 4-C or 4-D). Bold print shows anomalies: ratios that (at left) are predicted but not observed or ratios that (at right) are observed but not predicted.
predictions

|  | $A I$ | $A N$ | $B I$ | $B N$ |
| :--- | :---: | :---: | :---: | :---: |
|  | 8000 | 8000 | 8000 | 8000 |
| AI | 6200 | 4400 | 6200 | 4400 |
|  | 6020 | 6020 | 4040 | 4040 |
|  | $\mathbf{9 3 3 1}$ | $\mathbf{3 3 1 1}$ | $\mathbf{3 1 3 1}$ | $\mathbf{2 2 2 2}$ |
|  | 8000 | 0800 | 8000 | 0800 |
| AN | 4400 | 0602 | 4400 | 0404 |
|  | 6020 |  | 4040 |  |
|  | $\mathbf{3 3 1 1}$ |  | 2222 |  |
|  | 8000 | 8000 | 0080 | 0080 |
| BI | 6200 | 4400 | 0062 | 0044 |
|  | 4040 | 4040 |  |  |
|  | $\mathbf{3 1 3 1}$ | 2222 |  |  |
|  |  |  |  |  |
| BN | 8000 | 0800 | 0080 | 0008 |
|  | 4400 | 0404 | 0044 |  |
|  | $\mathbf{2 2 2 2}$ |  |  |  |
|  |  |  |  |  |

observations

|  | AI | AN | BI | BN |
| :--- | :---: | :---: | :---: | :---: |
|  | 8000 | 8000 | 8000 | 8000 |
|  | 6200 | 4400 | 6200 | 4400 |
| AI | 6020 | 6020 | 4040 | 4040 |
|  | $\mathbf{4 2 2 0}$ | $\mathbf{4 2 0 2}$ | $\mathbf{4 0 2 2}$ | $\mathbf{4 0 0 4}$ |
|  | $\mathbf{6 0 0 2}$ | $\mathbf{2 4 2 0}$ | $\mathbf{2 2 4 0}$ | $\mathbf{0 4 4 0}$ |
|  | 8000 | 0800 | 8000 | 0800 |
|  | 4400 | 0602 | 4400 | 0404 |
| AN | 6020 |  | 4040 |  |
|  | $\mathbf{4 2 0 2}$ |  | 2222 |  |
|  | $\mathbf{2 4 2 0}$ |  |  |  |
|  | 8000 | 8000 | 0080 | 0080 |
|  | 6200 | 4400 | 0062 | 0044 |
| BI | 4040 | 4040 |  |  |
|  | $\mathbf{4 0 2 2}$ | 2222 |  |  |
|  | $\mathbf{2 2 4 0}$ |  |  |  |
|  | 8000 | 0800 | 0080 | 0008 |
|  | 4400 | 0404 | 0044 |  |
| BN | 4040 |  |  |  |
|  | $\mathbf{4 0 0 4}$ |  |  |  |
|  | $\mathbf{0 4 4 0}$ |  |  |  |

Figure 19 (continued)

OView 4-G: Predicted results for phenotype crosses, based on the data in OView 0-A. The numbers shows the predicted percentages of B and N for each trait-cross. For example, for AxA there is a " 25 or 0 " to show that the predicted result is "either $25 \%$ B (and therefore $75 \% \mathrm{~A}$ ) or $0 \% \mathrm{~A}$ (and $100 \%$ B)."

|  | AI | AN | BI | BN |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| AI | AxA: 25 or 0 | AxA: 25 or 0 | AxB: 50 or 0 | AxB: 50 or 0 |
|  | IxI: 25 or 0 | IxN: 50 or 0 | IxI: 25 or 0 | IxN: 50 or 0 |
| AN | AxA: 25 or 0 | AxA: 25 or 0 | AxB: 50 or 0 | AxB: 50 or 0 |
|  | NxI: 50 or 0 | NxN 100 | NxI: 50 or 0 | NxN: 100 |
| BI | BXA: 50 or 0 | BxA: 50 or 0 | BxB: 100 | BxB: 100 |
|  | IxI: 25 or 0 | IxN: 50 or 0 | IxI: 25 or 0 | IxN: 50 or 0 |
| BN | BxA: 50 or 0 | BxA: 50 or 0 | BxB: 100 | BxB: 100 |
|  | NxI: 50 or 0 | NxN: 100 | NxI: 50 or 0 | NxN: 100 |

OView 4-H: Predicted phenotype data for all phenotype-combinations shown in OView 4-A.

|  | AI |  |  | AN |  | BI |  |  |  | BN |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | \%B | \% N | data | \%B | \% N | data | \%B | \%N | data | \% B | \%N | data |
| AI | 25 | 25 | 8000 | 25 | 50 | 8000 | 50 | 25 | 8000 | 50 | 50 | 8000 |
|  | 25 | 0 | 6200 | 25 | 0 | 4400 | 50 | 0 | 6200 | 50 | 0 | 4400 |
|  | 0 | 25 | 6020 | 0 | 50 | 6020 | 0 | 25 | 4040 | 0 | 50 | 4040 |
|  | 0 | 0 | 9331 | 0 | 0 | 3311 | 0 | 0 | 3131 | 0 | 0 | 2222 |
| AN | 25 | 50 | 8000 | 25 | 100 | 0800 | 50 | 50 | 8000 | 50 | 100 | 0800 |
|  | 25 | 0 | 4400 | 0 | 100 | 0602 | 50 | 0 | 4400 | 0 | 100 | 0404 |
|  | 0 | 50 | 6020 |  |  |  | 0 | 50 | 4040 |  |  |  |
|  | 0 | 0 | 3311 |  |  |  | 0 | 0 | 2222 |  |  |  |
| BI | 50 | 25 | 8000 | 50 | 50 | 8000 | 100 | 25 | 0080 | 100 | 50 | 0080 |
|  | 50 | 0 | 6200 | 50 | 0 | 4400 | 100 | 0 | 0062 | 100 | 0 | 0044 |
|  | 0 | 25 | 4040 | 0 | 50 | 4040 |  |  |  |  |  |  |
|  | 0 | 0 | 3131 | 0 | 0 | 2222 |  |  |  |  |  |  |
| BN | 50 | 50 | 8000 | 50 | 100 | 0800 | 100 | 50 | 0080 | 100 | 100 | 0008 |
|  | 50 | 0 | 4400 | 0 | 100 | 0404 | 100 | 0 | 0044 |  |  |  |
|  | 0 | 50 | 4040 |  |  |  |  |  |  |  |  |  |
|  | 0 | 0 | 2222 |  |  |  |  |  |  |  |  |  |

Figure 20: A Super-Punnett Overview for a " 3 alleles per individual" theory.

|  |  | aaaa | aad |  | add |  | $\begin{gathered} \text { ddd } \\ \mathbf{d} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | a | d | a | d |  |
| aaa | aa |  | $\begin{gathered} \mathrm{aaa} \\ \mathrm{~A} \\ \hline \end{gathered}$ | $\begin{gathered} \text { aaa } \\ \text { A } \end{gathered}$ | $\begin{gathered} \text { aad } \\ \text { B } \\ \hline \end{gathered}$ | $\begin{gathered} \text { aaa } \\ \text { A } \end{gathered}$ | $\begin{gathered} \mathrm{aad} \\ \mathrm{~B} \end{gathered}$ | aad B |
| aad | aa | $\begin{gathered} \mathrm{aaa} \\ \mathrm{~A} \end{gathered}$ | $\begin{gathered} \mathrm{aaa} \\ \mathrm{~A} \end{gathered}$ | $\begin{gathered} \text { aad } \\ \text { B } \\ \hline \end{gathered}$ | $\begin{gathered} \text { aaa } \\ \text { A } \\ \hline \end{gathered}$ | $\begin{gathered} \text { aad } \\ \text { B } \end{gathered}$ | aad B |
|  | ad | $\begin{gathered} \text { ada } \\ \text { B } \\ \hline \end{gathered}$ | $\begin{gathered} \mathrm{ada} \\ \mathrm{~B} \\ \hline \end{gathered}$ | add C | $\begin{gathered} \text { ada } \\ \text { B } \\ \hline \end{gathered}$ | $\begin{gathered} \hline \text { add } \\ \text { C } \\ \hline \end{gathered}$ | add <br> C |
| add | ad | $\begin{gathered} \text { ada } \\ \text { B } \\ \hline \end{gathered}$ | $\begin{gathered} \text { ada } \\ \text { B } \\ \hline \end{gathered}$ | $\begin{gathered} \text { add } \\ \text { C } \\ \hline \end{gathered}$ | $\begin{gathered} \text { ada } \\ \text { B } \\ \hline \end{gathered}$ | $\begin{gathered} \text { add } \\ \text { C } \\ \hline \end{gathered}$ | $\begin{gathered} \text { add } \\ \mathrm{C} \\ \hline \end{gathered}$ |
|  | dd | $\begin{gathered} \mathrm{dda} \\ \mathrm{C} \end{gathered}$ | $\begin{gathered} \mathrm{dda} \\ \mathrm{C} \\ \hline \end{gathered}$ | $\begin{gathered} \text { ddd } \\ \text { D } \\ \hline \end{gathered}$ | $\begin{gathered} \mathrm{dda} \\ \mathrm{C} \\ \hline \end{gathered}$ | $\begin{gathered} \text { ddd } \\ \text { D } \\ \hline \end{gathered}$ | $\begin{gathered} \hline \text { ddd } \\ \text { D } \\ \hline \end{gathered}$ |
| ddd | dd | $\begin{gathered} \hline \text { dda } \\ \text { C } \end{gathered}$ | $\begin{gathered} \hline \text { dda } \\ \text { C } \end{gathered}$ | $\begin{gathered} \text { ddd } \\ \text { D } \end{gathered}$ | dda C | ddd | $\begin{gathered} \hline \text { ddd } \\ \mathrm{D} \end{gathered}$ |

Figure 21: A Summary of Research on GCK-based Problem Solving

|  | date of <br> study | date <br> of <br> dissrt <br> n | GCK <br> used <br> $?$ | at <br> MG? | interpretiv <br> e <br> framework | individuals <br> or groups? | skill <br> level | focus of <br> research |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Collins | - | 1986 | yes | no | Reif (PS) | individuals | novice | strategies |
| Thomson | - | 1993 | yes | no | Darden | individuals | expert | strategies |
| Hafner | 1990 | 1991 | yes | yes | MRPSG | individuals | novice | strategies |
| Finkel | 1992 | 1993 | yes | yes | Sociology <br> of Science | groups | novice | interactions <br> \& strategies |
| Wynne | 1993 | 1995 | yes | yes | Clement,... | groups | novice | strategies |
| Lem- <br> berger | 1994 | 1995 | yes | yes | Conceptual <br> Change | groups | novice |  <br> instruction |
| Johnson | 1992 | 1996 | yes | yes | Darden | groups | novice | strategies |
| Rusbult | $1992-94$ | 1997 | yes | yes | ISM | groups | novice | instruction |

Figure 22: The relative complexity of models proposed by students.

| my name <br> for the <br> model | alleles in <br> populatio <br> n | alleles in <br> individual | number of <br> phenotypes | number of <br> genotypes | total <br> number <br> of crosses | non- <br> duplicate <br> crosses |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2-and-2 | 2 | 2 | 2 or 3 | 3 | 9 | 6 |
| 3-and-2 | 3 | 2 | 3 to 6 | 6 | 36 | 21 |
| 4-and-2 | 4 | 2 | 4 to 10 | 10 | 100 | 55 |
| 2-and-3 | 2 | 3 | 2 to 4 | 4 | 72 | 36 |
| 3-and-3 | 3 | 3 | 3 to 10 | 10 | 648 | 324 |
| 4-and-3 | 4 | 3 | 4 to 20 | 20 | 3200 | 1600 |
| 4-and-4 | 4 | 4 | 4 to 35 | 35 | 2450 | 1225 |

The "total number of non-duplicate crosses" refers to either crosses where genotypes vary (for models with 2 alleles per individual) or to crosses where the genotypes and/or phenotypes vary (for models with 3 or 4 alleles per individual), as explained in Section B15.

Section B15 contains a Prediction Overview, with accompanying explanation, for an easy way to represent the 36 crosses in the ' 2 -and- 3 ' model. A similar system can be used for the other models that have 3 or 4 alleles per individual, although it is questionable whether there can be an "easy" way to do the 324 crosses (or more!) that are possible for these models.

